Correlation of Coronal Mass Ejection Shock Temperature with Solar Energetic Particle Intensity

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ABSTRACT

Solar energetic particle (SEP) events have been observed by the Parker Solar Probe (PSP) spacecraft since its launch in 2018. These events include sources from solar flares and coronal mass ejections (CMEs). Onboard PSP is the IS \odot IS instrument suite measuring ions over energies from ~ 20 keV/nucleon to 200 MeV/nucleon and electrons from ~ 20 keV to 6 MeV. Previous studies sought to group CME characteristics based on their plasma conditions and arrived at general descriptions with large statistical errors, leaving open questions on how to properly group CMEs based solely on their plasma conditions. To help resolve these open questions, plasma properties of CMEs have been examined in relation to SEPs. Here we reexamine one plasma property, the solar wind proton temperature, and compare it to the proton SEP intensity in a region immediately downstream of a CME-driven shock for seven CMEs observed at radial distances within 1 au. We find a statistically strong correlation between proton SEP intensity and bulk proton temperature, indicating a clear relationship between SEPs and the conditions in the solar wind. Furthermore, we propose that an indirect coupling of SEP intensity to the level of turbulence and the amount of energy dissipation that results is mainly responsible for the observed correlation between SEP intensity and proton temperature. These results are key to understanding the interaction of SEPs with the bulk solar wind in CME-driven shocks and will improve our ability to model the interplay of shock evolution and particle acceleration.

Keywords: Solar energetic particles, Solar coronal mass ejection shocks, solar wind

1. INTRODUCTION

Coronal mass ejections (CMEs) are solar events involving the expulsion of large amounts of solar coronal material into interplanetary space. These events are observed to have wide variability in their characteristics, such as their composition, magnetic field strength and behavior, in-situ plasma conditions, and shock strengths. Many of these characteristics have been studied resulting in an array of expectations that vary from one CME to the next (Cane et al. 1990; Gosling et al. 1991; Neugebauer et al. 1997; Zurbuchen & Richardson 2006; Richardson & Cane 2010; Wu & Lepping 2011; Chi et al. 2016, and references therein). A recent investigation into the turbulence properties of CME cores inside 1 au (Good et al. 2023) via Solar Orbiter and Parker Solar Probe (PSP) observations revealed radial trends in the magnetic turbulent energy and the inertial-to-dissipative range break-point frequency, which is analogous to the dissipation scale where turbulent energy cascaded from larger to smaller scales can dissipate as heat. These authors further demonstrated the variability of other CME characteristics, such as plasma beta (ratio of thermal to

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magnetic pressure) and correlation length, leaving an open question on how to properly group CMEs based solely on their plasma properties.

To better group CMEs, their plasma properties have been examined in relation to solar energetic particles (SEPs). CMEs can drive an upstream forward propagating shock if they are traveling faster than the upstream solar wind by at least the local fast magnetosonic speed, where the upstream plasma is unshocked and the downstream plasma is shocked. These CME-driven shocks become a source for particle acceleration (Lee 1997) with variable efficiency in their acceleration processes (Kallenrode 1996; Lario et al. 1998), where turbulent diffusion is thought to produce the shock's dominant particle acceleration process (Fisk 1971; Axford et al. 1977; Blandford & Ostriker 1978; Bell 1978; Gosling et al. 1979; Lee 1983). Noticeable increases in the suprathermal particle population (energies generally between ~ 10 keV to ~ 1 MeV per nucleon (Mason & Gloeckler 2012)) and of those with higher energy at CME-driven shocks are the result of these local acceleration processes (Reames 1999). CME-driven shock speeds have been found to be correlated with peak SEP flux at the shock (Cane et al. 1990; Reames 2000; Kahler 2001) for higher energies (> 10 MeV), with considerable scatter. This correlation can be explained by the association of stronger shocks with more intense CMEs resulting in a larger SEP flux of higher energy particles. Nonetheless, the considerable scatter over several decades of SEP intensity for a given range of CME speeds suggests the peak SEP flux is also dependent on other factors besides the CME speed, such as the ambient SEP population (Kahler 2001). When considering the behavior of the peak energetic particle (EP) intensity in the heliosheath, Zank et al. (2015) found that the EP intensity peaks downstream of the heliospheric bow shock and the distance between the shock and this peak increases with increasing particle energy.

One method used to characterize the relationship between SEPs and turbulence is the partial variance of increments (PVI) (Greco et al. 2008), a measure of turbulence intermittency or roughness of the magnetic field at a given increment scale, which is found to be well-correlated with solar wind temperature (Osman et al. 2011, 2012; Greco et al. 2012; Chasapis et al. 2015; Yordanova et al. 2016; Qudsi et al. 2020). Additionally, Tessein et al. (2013, 2015) and Bandyopadhyay et al. (2020) found a correlation between PVI and SEP intensity, where others discovered an association between local acceleration regions and magnetic-like islands formed due to turbulence (Khabarova et al. 2015; Khabarova & Zank 2017; Malandraki et al. 2019). Although PVI and SEP intensity are correlated on average, there are instances where SEP enhancements are observed at times with low PVI. These times with larger SEP intensity, however, are bounded by high PVI, suggesting that coherent structures play a role in the local modulation and trapping of energetic particles (Tessein et al. 2015; Pecora et al. 2021).

Based on the outcomes of the observational studies above, one might expect SEP intensity can be used to gauge the solar wind proton temperature, a connection motivated by the relation between SEP intensity and shock strength. From the perspective of theory and modeling, the influence of the upstream turbulence level and presence of coherent structures are found to result in more efficient diffusive-like spreading of particles in both position and velocity space (Trotta et al. 2021). Furthermore, the level of upstream turbulence induces shock-surface fluctuations and downstream turbulence structuring that have been linked to temperature anisotropy downstream of the shock (Trotta et al. 2023). However, there are no studies to date that have directly investigated the relationship between the bulk proton temperature immediately downstream of CME-driven shocks and the intensity of suprathermal particle populations locally accelerated by turbulent diffusion near the shock (although, see Dayeh et al. (2018) and the inferred results of Lario et al. (2017)). The shock strength and turbulence strength near the shock are found to be well-correlated, where turbulence is known to affect SEP transport (Jokipii 1982, 1987; Dröge 1994; Guo et al. 2021). This natural interaction between SEPs and turbulence near the shock may also be reflected in the proton temperature, since intermittency results in increased heating of the bulk material at the targeted scales.

In this paper, we examine the relationship of proton temperature and particle intensity through the analysis of SEP and in-situ plasma measurements by PSP (Fox et al. 2016) for seven CME-driven shocks. In Section 2, we explain the data and methods used to reach the results in Section 3. We discuss the results and their impact on the understanding of SEP interactions with the bulk solar wind in shocks in Section 4. Finally, we summarize the results in Section 5.

2. DATA AND METHODS

We utilize publicly available measurements of solar energetic particles via PSP/IS \odot IS EPI-Lo (McComas et al. 2016), magnetic field data via PSP/FIELDS (Bale et al. 2016), and proton temperatures, bulk velocity, and proton density via PSP/SWEAP/SPAN-I (Kasper et al. 2016) from NASA's Space Physics Data Facility¹. We identify possible shock candidates from the FIELDS and SWEAP data and identify the relevant one by comparing its time to the estimated shock arrival time. Estimated shock arrival times are found by first considering their associated type-II radio bursts (Bale et al. 1999; Knock et al. 2001; Mann & Klassen 2005), measured by PSP/FIELDS, adjusted to solar origin, denoted by time t_0 . The time of solar origin is determined by subtracting

¹ Space Physics Data Facility can be accessed at https://cdaweb.gsfc.nasa.gov/.

the travel time of light from the Sun to the radial distance of PSP from the time of the observed radio-II burst. Next, we find the time associated with the propagation of the CME-driven shock (estimated by the WSA-ENLIL model (Odstrčil et al. 1996; Odstrčil & Pizzo 1999a,b; Odstrčil 2003; Odstrčil et al. 2004) for each shock separately) starting from a solar origin to the radial distance of PSP, denoted as time t_1 . Then we select the nearest shock candidate to the time $t_0 + t_1$. This gives us a total of seven CME-driven shocks, overviews of which can be found in the Appendix (Figure A.4), with vertical dashed red lines used to mark the corresponding shock arrivals.

To reinforce the connection between SEP intensity and proton temperature via turbulent processes, we compute the PVI of the magnetic field downsampled to 1 second cadence from the native '4_Sa_per_Cyc' data product. The PVI is defined in Greco et al. (2008) as

$$PVI(t,\tau) = \frac{|\Delta \boldsymbol{B}(t,\tau)|}{\sqrt{\langle |\Delta \boldsymbol{B}(t,\tau)|^2 \rangle}}$$
(1)

where $\Delta B(t, \tau) = B(t + \tau) - B(t)$ is the increment of magnetic field vector **B** at time t and temporal increment scale τ , and the brackets $\langle \cdot \rangle$ represent an arithmetic mean. We choose an increment scale of 10 seconds, which is shorter than that used in Bandyopadhyay et al. (2020) due to the availability of higher resolution magnetic field data and is in the inertial range far from the correlation scale but larger than the dissipative scale.

The duration of the arithmetic mean used in the normalization of PVI varies from event to event. To determine this duration, we first compute the auto-correlation function:

$$R(\tau) = \frac{\langle \boldsymbol{b}(t) \cdot \boldsymbol{b}(t+\tau) \rangle_t}{\langle \boldsymbol{b}(t) \cdot \boldsymbol{b}(t) \rangle_t}$$
(2)

where $\mathbf{b}(t) = \mathbf{B}(t) - \langle \mathbf{B}(t) \rangle_t$ is the fluctuating component of the magnetic field and $\langle \cdot \rangle_t$ is computed via the Germano approach (Germano 1992). The interval duration used in Equation (2) is set at 16 hours centered about the estimated shock arrival time, which is an appropriate interval duration at 1 au (Isaacs et al. 2015). The value of τ_c such that $R(\tau = \tau_c)$ drops below e^{-1} is the "e-folding" time or correlation time (Matthaeus et al. 1999). We then set the duration of the arithmetic mean used in the normalization of PVI to $10 \cdot \tau_c$ centered about the estimated shock arrival time.

However, in this study, PSP encounters each of the CME-driven shocks within 1 au where the correlation scale is expected to be shorter, on average, which presumably calls for shorter averaging intervals when computing magnetic correlations. Therefore, assuming a 16 hour duration will lead to an overestimated correlation scale and a larger averaging duration used for normalizing the PVI. Although this is important with investigations that directly depend on the correlation scale, an averaging duration for the PVI normalization beyond 10 times the actual correlation scale is found to insignificantly affect PVI enhancements (Servidio et al. 2011). Once the PVI($\tau = 10$ seconds) is obtained, we compute the fraction of PVI values, denoted as PVI_{frac}, greater than 2.5 only within the duration used for time-integration and averaging of the energy-integrated intensity and proton temperature, respectively. This threshold is selected since coherent structures are associated with PVI values greater than 2.5 (Greco et al. 2008, 2012, 2018).

To compute the SEP intensity of protons shown below in Section 3, we examine proton intensities measured by the EPI-Lo instrument. EPI-Lo is comprised of 8 wedges, each with 10 apertures having different look directions (Hill et al. 2017). Here we utilize all apertures that are unaffected by dust puncture events on EPI-Lo (Szalay et al. (2020); Shen et al. (2023, in prep.)) to account for the changing magnetic field direction (or changing pitch angle, the angle between the observed particle's incident direction and the instantaneous magnetic field direction) during CME shock passage. The data product used in this study is Channel P, which corresponds to protons with triple coincidence measurements (Hill et al. 2017).

We first integrate the measured flux (*F*) over the energy (*E*) domain (100 keV to 500 keV), normalized by the summation of the energy bin widths to properly account for energy bin weights. This results in an energy-integrated flux ($F_E(t)$) defined as

$$F_E(t) = \frac{\sum_{100\text{keV}}^{500\text{keV}} [\Delta E_i \cdot F(t, E_i)]}{\sum_{100\text{keV}}^{500\text{keV}} [\Delta E_i]}$$
(3)

where ΔE_i is the energy bin width associated with the measured flux at energy E_i . We then integrate $F_E(t)$ over the time domain for a duration equivalent to $3 \cdot \tau_c$, which is expected to vary from event to event. We choose this duration to (1) constrain the results to describe the downstream region nearest to the shock and (2) include magnetic structures large enough to capture the acceleration of and/or systematic trapping of energetic particles. For event-to-event comparisons, we normalize time integration by the duration of the integration. We also confirmed that the qualitative results and strength of correlation between any pair of

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parameters (proton temperature, proton SEP intensity, and PVI_{frac} ; see Appendix, Table 1) are not sensitive to our exact choice of time window; changing the durations of the window from 0.5 to $5 \cdot \tau_c$ only insignificantly affects the results.

This results in a time and integrated measured flux in units of $(cm^2 \cdot sr \cdot s \cdot keV/nuc)^{-1}$, defined as

$$F_{E,t} = \text{Intensity} = \frac{\sum_{t_s}^{t_s + 3\tau_c} [\Delta t \cdot F_E(t)]}{\sum_{t_s}^{t_s + 3\tau_c} [\Delta t]}$$
(4)

where t_s is the time of the CME-driven shock. For the rest of the paper, we interchangeably use the terms 'flux' and 'intensity' to describe the value $F_{E,t}$ where it does not cause confusion. We compare the resulting proton SEP intensity to the proton temperature T_p measured by SPAN-I from PSP/SWEAP in its native time resolution, averaged over the same duration of $3 \cdot \tau_c$ downstream of the CME-driven shock.

One challenge is that instrument uncertainties in SPAN-I proton temperatures are unavailable. Therefore, we assume an uncertainty of each measurement of 20% (Kasper et al. 2016), which is a reasonable estimate for the radial distances at which PSP observed the CMEs (~ 0.35 au to .80 au) and the SPAN-I field-of-view throughout the averaging duration. Quality flags in the SPAN-I data product are checked to ensure reasonable confidence in the measured value. Also, we impose one condition on the data for the SEP event to be considered for analysis: data availability throughout the passing of a CME-driven shock by all three instrument suites (IS \odot IS/FIELDS/SWEAP). Several CME-driven shocks, beyond those included here, observed by PSP/IS \odot IS were rendered unusable for the present analysis due to data gaps from instrument turn-offs and spacecraft rolls for satellite repositioning during the shock encounter.

3. RESULTS

Here we compile the shock intensity and proton temperature for seven different CMEs, with event overviews provided in the Appendix, Figure A.4. In Figure 1, we provide an example of the analysis for the Feb. 15, 2022, CME event. The top panel shows energy-integrated proton intensities ($F_E(t)$) over energies 100 keV to 500 keV, the middle panel shows bulk proton temperatures, and the bottom panel shows PVI at a 10 second increment. The vertical dashed red line corresponds to the estimated shock arrival time, for which each curve is adjusted. The duration between the estimated shock arrival time and the vertical solid black line corresponds to the time window used to compute $F_{E,T}$ and average proton temperature (in this case, $3 \cdot \tau_c$). Parameters of average proton temperature ($\langle T_p \rangle$), proton SEP intensity, and PVI_{frac} over a $3 \cdot \tau_c$ duration for the seven CME events are given in the Appendix, Table 2.

The compiled values of the intensity and proton temperature are shown in the left panel of Figure 2 for the selected duration of $3 \times \tau_c$. The horizontal error bars represent the propagated error throughout the time and energy integrated intensity, and the vertical error bars represent the propagated error from the proton temperatures. We utilize an orthogonal distance regression (ODR; Boggs & Rogers 1990) power-law fit between the proton SEP intensity and $\langle T_p \rangle$, which considers uncertainty in dependent and independent variables, only to show the proportionality between the two parameters (left panel of Figure 2). The fitted slope and standard error are given in the corresponding legend. In the middle and right panels of Figure 2, we examine the behavior of proton SEP intensity and proton temperature as a function of PVI_{frac} , respectively. An arrow is drawn in the middle and right panels of Figure 2 only to further demonstrate the relationship between PVI and either $\langle T_p \rangle$ or SEP intensity; regions with proportionately enhanced PVI are associated with regions of hotter bulk plasma and larger SEP intensity.

Figure 2 reveals correlations between SEP intensity, bulk proton temperature, and PVI_{frac} downstream of the shock over a duration of $3 \cdot \tau_c$. While there is only a small statistical sample via PSP observations due to constraints on data availability, the correlation coefficients (*r*) of $\log \langle T_p \rangle$ to log Intensity, log Intensity to $\log PVI_{frac}$, and $\log \langle T_p \rangle$ to $\log PVI_{frac}$ are 0.95, 0.81, and 0.81, respectively, which all correspond to statistically strong correlations (Taylor 1990). In the Appendix, Table 1, we provide the correlation coefficients for various durations downstream of the CME-driven shock, which shows insignificant changes in the correlation coefficients between any two parameters. The results here demonstrate that the proton SEP intensity can be used to gauge the bulk proton temperature in the downstream region of CME-driven shocks.

4. DISCUSSION

We provide an illustration (Figure 3) to help visualize our explanations of the observed results that we discuss below. Figure 3 has real data of a CME-driven shock crossing by PSP for the Feb. 15, 2022, CME event accompanied by an illustration depicting the structure of a CME and a sample trajectory across its associated shock.

An interpretation of the results presented in Figure 2 involves the level of turbulence and the shock strength. Suprathermal particles can be trapped and/or modulated by the emergence of coherent structures, increasing the amount of time they spend in the diffusive shock region, which are visualized in the illustration of Figure 3. If these particles remain sufficiently trapped,

then one might expect a larger intensity of particles observed at that shock. This property reflects the acceleration efficiency of the shock and the level of turbulence in these regions, resulting in elevated energy dissipation (heating) due to the emergence of coherent structures, as can be measured via PVI (Qudsi et al. 2020, and references therein). In fact, the PVI shown in Figures 1 and A.4 reveal enhanced values of PVI in the selected region downstream of the shock, corroborating the correlation of PVI and SEP intensity (Tessein et al. 2013, 2015; Bandyopadhyay et al. 2020) and/or the effectiveness of coherent structures in locally modulating/trapping energetic particles (Mazur et al. 2000; Ruffolo et al. 2003; Kittinaradorn et al. 2009; Tessein et al. 2016; Khabarova et al. 2021; Pezzi et al. 2021; Pecora et al. 2021). Additionally, the correlation coefficients between all possible pairs of PVI, proton temperature, and SEP intensity indicate statistically strong correlations. As a result, the SEP intensity enables an inference of the proton temperature from the increased heating due to turbulence intermittency.

Supplementing the above interpretation, an increased intensity at the shock can also be explained by the bulk temperature and its impact on the efficiency of particle injection at shocks. High bulk temperatures increase the likelihood for particles to have sufficient speed to move upstream and thereby become injected into diffusive shock acceleration (Gloeckler & Geiss 1998; Chotoo et al. 2000; Zurbuchen et al. 2000). This dynamic can be visualized in Figure 3 where particles move towards the upstream plasma and get picked up into diffusive shock acceleration. This is due to the increased bulk temperature raising the thermal core closer to the suprathermal energies, enabling an increased seed population for acceleration and/or trapping within the diffusion region. Given the current results, this implies a strong interplay between solar wind temperature, injection efficiency, and SEP intensity.

Considerations of other well-correlated properties of CME-driven shocks with SEP intensity, such as shock normal relative to the magnetic field (Lario et al. 2016; Giacalone 2017; Chen et al. 2022), radial distance from the Sun due to the weakening of such shocks (Salman et al. 2020), and connection to the shock (Burlaga et al. 1981; Kilpua et al. 2011; Möstl et al. 2009) may influence the present results. However, many of these other properties are associated with the shock strength, which is an

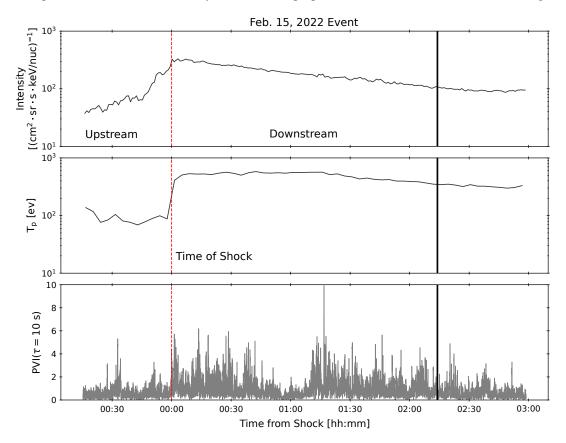


Figure 1. Energy-integrated proton intensity over energies 100 keV to 500 keV (top), solar wind proton temperature (middle), and $PVI(\tau = 10 \text{ seconds})$ (bottom) centered about a $3 \cdot \tau_c$ duration marked between the shock arrival (vertical dashed red line) and the vertical dashed black line associated with the Feb. 15, 2022, CME event.

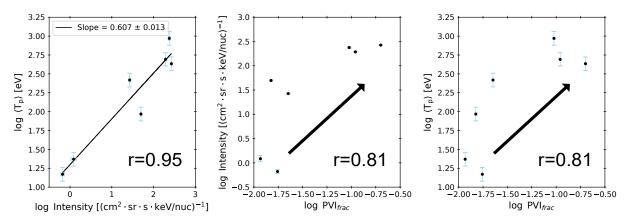


Figure 2. Compiled solar wind $\langle T_p \rangle$, proton SEP intensity, and PVI_{*frac*} each as a function of the other (black circles) in the region immediately downstream of the appropriate CME-driven shock. In the left panel, vertical error bars are propagated standard errors from averaged temperatures and horizontal error bars are propagated uncertainties from time and energy integrated proton flux. The solid black line is an ODR power-law fit to show proportionality. The correlation coefficients (r) of the parameters in the left, middle, and right panel are 0.95, 0.81, and 0.81, respectively. Arrows in the middle and right panels are to express a general trend.

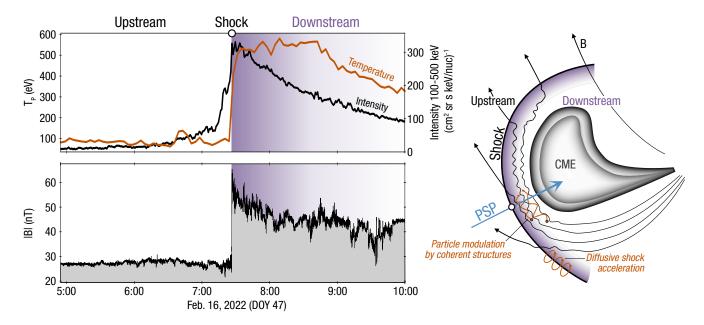


Figure 3. Illustration of CME structure with PSP crossing its driven shock. The top panel shows the measured proton flux integrated over energy (100 keV to 500 keV) and proton temperature; the bottom panel shows the magnetic field magnitude. The CME-driven shock encounter is labeled on PSP's sketched trajectory as an open circle, which corresponds to the open circle on the top axis of the top panel. The trajectory shows PSP traversing the upstream region, encountering the shock, and then observing the downstream plasma. Sketch of CME structure is adapted from Cane (2000).

indicator of the efficiency in acceleration processes due to the turbulent nature downstream of the shock. Therefore, we only consider the individual connections of the intensity and temperature to the level of turbulence in the downstream region.

5. CONCLUSION

In this paper, we investigate the relationship between shock proton temperature with shock associated particle intensity. The intensity to temperature correlation had previously only been inferred by existing correlations of PVI, a measure of turbulence intermittency, to both intensity and temperature, separately. Our results (Figure 2) suggest the proton SEP intensity can be used to gauge whether one would expect a larger or smaller proton temperature immediately downstream of a CME-driven shock. We

compute the PVI to help strengthen the explanations relating the SEP intensity to the proton temperature, which reveals enhanced PVI in the downstream region.

The results presented here will likely improve the understanding and modeling of SEP interactions with shocks and the downstream bulk plasma. Additional spacecraft observations of SEPs and proton temperatures can be used to significantly increase the statistical significance of these results and possibly examine their radial profiles. The correction for radial weakening of shocks and temperature cooling due to expansion will need to be considered when examining the radial dependence of CME properties in general. Finally, as the Sun transitions into solar maximum, we anticipate an increase of observed CME-driven shocks in future PSP orbits that can be used to supplement the results presented here in addition supporting other systematic studies of CME-related phenomena.

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APPENDIX

A. SUPPLEMENTARY TABLES AND FIGURES

We consider cases of different durations used in the time-integration and averaging duration of the intensity and proton temperature, respectively. As shown in Table 1, changing this duration insignificantly alters the strength of correlation between any two parameters. We also provide the the correlation time and the values of proton temperature, SEP intensity, and PVI_{frac} from Figure 2 for each event, as shown in Table 2. These values in Table 2 correspond to a time-integration and averaging duration of $3 \cdot \tau_c$ immediately downstream of the CME-driven shock.

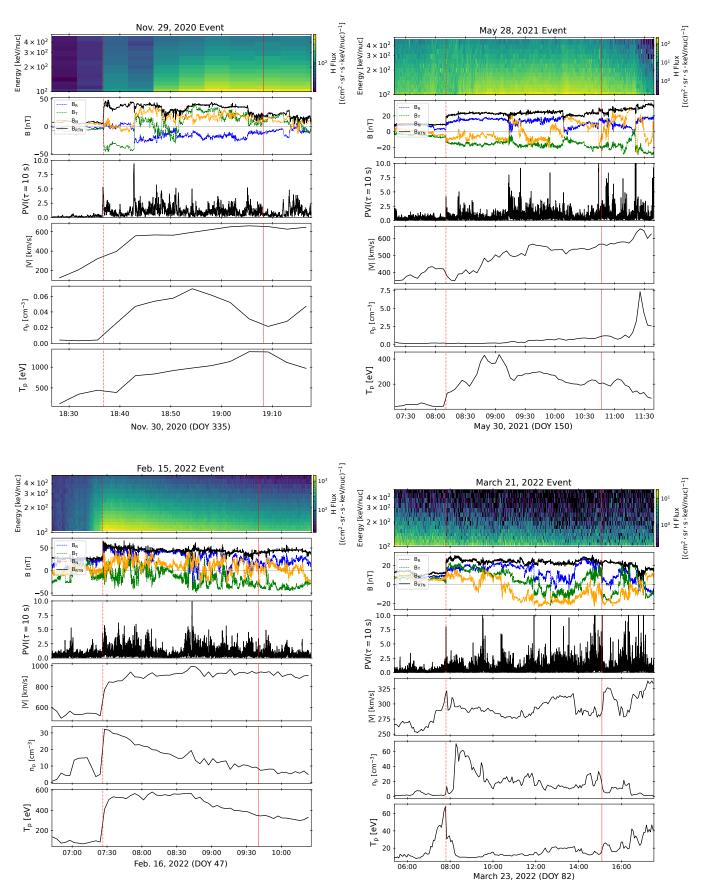
Correlation	$0.5 \cdot \tau_c$	$1 \cdot \tau_c$	$2 \cdot \tau_c$	$3 \cdot \tau_c$	$4 \cdot \tau_c$	$5 \cdot \tau_c$
$\log \langle T_p \rangle$ to log Intensity	0.94	0.92	0.94	0.95	0.96	0.95
log Intensity to log PVI frac	0.81	0.81	0.81	0.81	0.82	0.83
$\log \langle T_p \rangle$ to $\log PVI_{frac}$	0.87	0.84	0.82	0.81	0.79	0.81

Table 1. Correlation coefficients for the pair of parameters given in the first column for different time-integration/averaging duration. Overall, the correlations do not significantly alter across different duration based on factors of the correlation time τ_c .

		SEP Intensity		
Event	$\langle T_p \rangle$ [eV]	$\left[(\mathrm{cm}^2\cdot\mathrm{sr}\cdot\mathrm{s}\cdot\mathrm{keV}/\mathrm{nuc})^{-1}\right]$	PVI _{frac}	τ_c [s]
2020-11-29	933 ± 194	237.8 ± 8.9	0.09	630
2021-05-28	262 ± 54	26.7 ± 0.9	0.02	3130
2022-02-15	492 ± 99	193.4 ± 2.1	0.11	2680
2022-03-21	15 ± 3	0.7 ± 0.1	0.02	8730
2022-07-09	23 ± 5	1.2 ± 0.2	0.01	2880
2022-08-28	431 ± 89	266.4 ± 3.0	0.20	1730
2023-01-03	93 ± 19	49.8 ± 1.4	0.01	1530

Table 2. Values of $\langle T_p \rangle$, SEP intensity, PVI_{frac} , and τ_c for each event using a duration of $3 \cdot \tau_c$ for time-integration of the energy-integrated particle flux and averaging of T_p . These values are reflected in Figure 2.

Figure A.4 provides an overview of the seven events examined in this study. For each event, there are five panels that represent the EPI-Lo Channel P omni-directional proton flux spectrogram, magnetic field, $PVI(\tau = 10 \text{ seconds})$, magnitude of the bulk velocity, proton density, and proton temperature in descending order. The time range includes the estimated shock arrival time, marked by the vertical dashed red line. The time window used for integration of the energy-integrated intensity and averaging of the proton temperature is between the shock arrival time and the time marked by the vertical solid red line. These event overviews provide confirmation of data availability throughout these time periods.



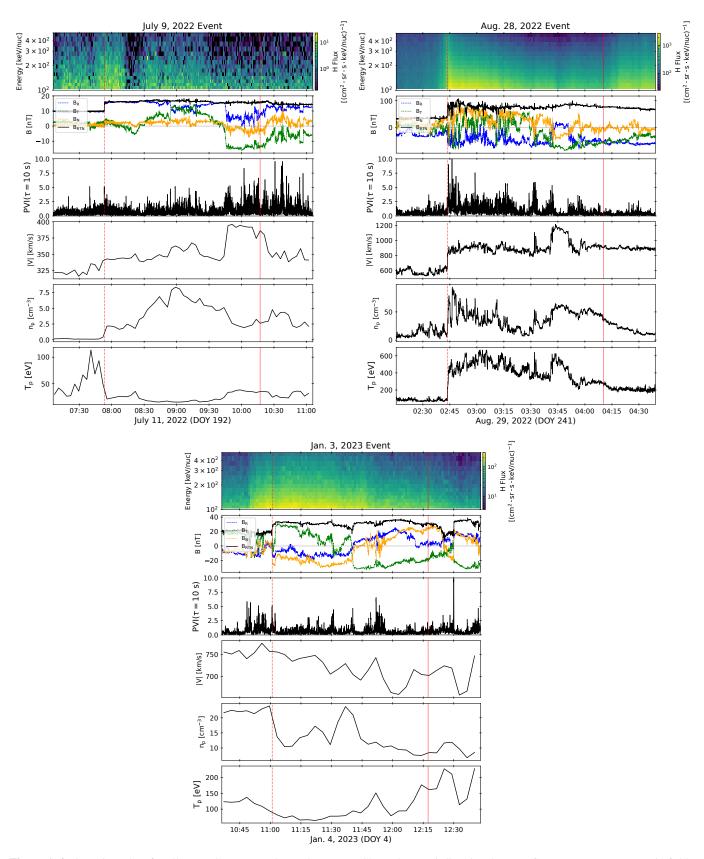


Figure A.4. Overview plots for all seven CMEs. Panels are the EPI-Lo Channel P omni-directional proton flux spectrogram, magnetic field, PVI at increment scale $\tau = 10$ seconds, bulk velocity, proton density, and proton temperature in descending order for each event. The vertical red dashed line in all panels represents the estimated CME shock arrival time for that corresponding event.

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